Math

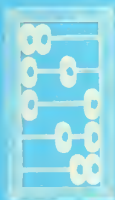UIUCDCS-R-79-957   UILU-ENG 79 1702

Final Report for the Navy for Contract N000014-75-C-0982

BURST PROCESSING

by

W. J. Poppelbaum
Principal Investigator

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DEPARTMENT OF COMPUTER SCIENCE
UNIVERSITY OF ILLINOIS AT URBANA-CHAMPAIGN · URBANA, ILLINOIS

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0. <u>ABSTRACT</u>

To multiply two numbers with 7 bit (i.e. 1%) accuracy a 2000
transistor microprocessor needs about 10 clock-periods. A stochastic
computer gives the same accuracy (within one standard deviation) in 10^4
clock periods--but it only uses a 2 transistor AND for the operation.
For the last 4 years the Information Engineering Laboratory in the
Department of Computer Science at the University of Illinois has examined
a "compromise" called BURST PROCESSING, which uses deterministic methods
(like a microprocessor), but averages (like a stochastic machine). The
fundamental idea is to perform 1-decimal digit arithmetic and to obtain
accuracy by averaging over various inputs. For example 3.4 would be
treated as 4444333333 and 6.2 as 7766666666. Using the insight that the
average of a sum is the sum of the averages, we can use a simple adder
which forms (4 + 7), etc., the average being 9.6 = 3.4 + 6.2!

The actual representation uses a unary PCM frame, e.g. 7
corresponds to a "burst" consisting of the (first) seven slots of a 10-
slot frame being filled. This has the advantage that, as long as the
number represented does not change, <u>it is immaterial which 10 adjacent
slots ("window") we look at</u>: A window contains always the same informa-
tion. Should the information change (e.g. from 2 to 8 occupied slots),
the contents of the window will increase steadily from the initial to
the final value. In practice it is useful to introduce so called block-

sum registers (BSR's) which look at 10 adjacent slots and put out a voltage proportional to the number of "ones" in the BSR.

Besides it's simplicity, burst processing has some additional advantages: There are no correlation difficulties as in stochastics, nor do we usually have to staticize the information as in a microprocessor. Also the burst format is only $2 \frac{1}{2}$ times less efficient in bandwidth requirements than weighted binary: It can be used directly for audio and video transmissions. The lost bandwidth is compensated for by good noise-immunity under very high noise conditions (i.e. as much as 10% error rate!). Lastly the accuracy of burst processing increases linearly with the number of slots, as contrasted with the square-root law of stochastics.

This report describes both a quasi-analog and a purely digital fashion of performing arithmetic using bursts. On the way the use of non-compacted bursts and the corresponding encoders is brought up. Then the general area of digital filters, realized in burst technology, is discussed and practical examples from the area of convolution, adaptive filtering and RF tuning and demodulation are given. Finally applications to picture processing and "spatial" versions of burst processing are mentioned and suggestions made for future areas of study.

1.   INTRODUCTION

     The field of computation and communication--initially purely
analog--has been almost entirely taken over by weighted binary (WB)
digital techniques, simply because the circuit parameter tolerances are
so much greater when one makes a binary decision on each pulse; also
the binary representation is relatively efficient. The advent of micro-
computers and packet switching only reinforced our belief in these binary
digital implementations and it may seem preposterous to even suggest
alternate, albeit digital, technologies. What we mean by "alternate" is
"non weighted binary" (NWB). Historically NWB systems have played an
important role: The earliest digital computers were digital differential
analyzers(DDA's) in which one simply counted the number of pulses (in a
given time or in a given number of time slots). A DDA uses therefore
a unary number representations: Each pulse is a marker and one counts
markers. Sometimes, of course, the count will have to be displayed--one
then uses a binary, octal, decimal or hexadecimal representation. When
the pulses are used in a control system (actuators for rudders, antennas
etc.) it is usually not necessary to specifically refer to a number system.

     More recently considerable success has been obtained by stochastic
or probabilistic unary encoding [-6][-5][-4][-3][-2][-1][0]. Here a number
is represented by the probability of appearance of a pulse in a given time
slot. The ultra-simplicity of the computational circuits in this stochastic
method is well know, as is the failsoft behavior: A pulse more or less does
not matter; Figure 1 shows a common way of multiplying by an AND and adding
by two AND's and an OR. The crux of the method is to assess the probabilities
by measuring the average frequency (the probability being the limit for an
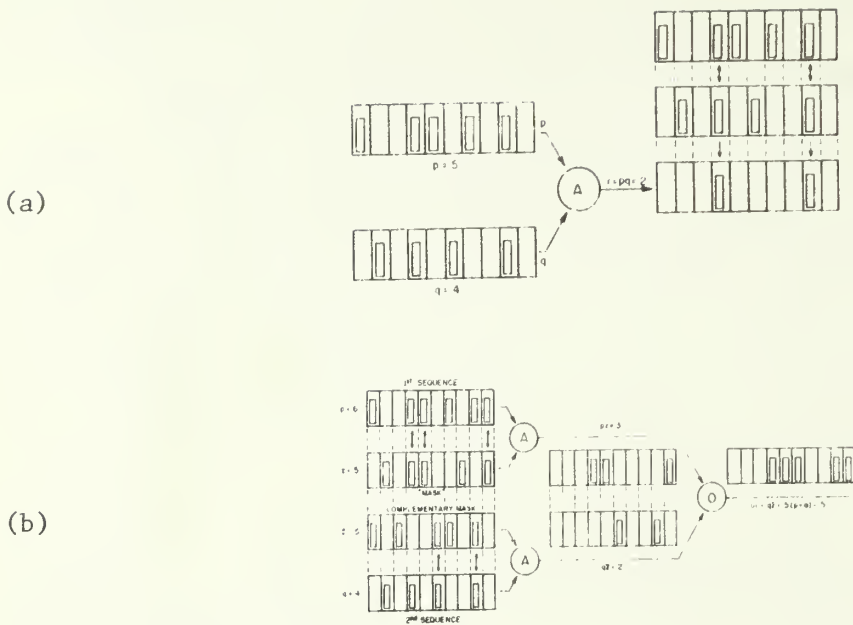infinite number of time-slot). Unfortunately [3] the number of time-slots

(a)

(b)

Figure 1

Stochastic Multiplication and Addition

to obtain 10% midrange-precision (with 68% likelihood) is 10^2, for 1% we need 10^4, for 0.1%, 10^6, i.e. the precision increases only as the square root of the number of time slots. Furthermore one must make quite sure that the random pulse sequences (RPS's) which represent 2 variables (to be processed) are uncorrelated. In practice there are many applications (e.g., stochastic feedback controls) in which 1% accuracy is quite sufficient. With a 10MHz clock this means a computation time of 10^{-3}s, an often acceptable value. Note also that negative numbers can be represented by mapping the interval -1,+1 onto the probabilities from 0 to +1. Lately transducers have been built which furnish directly RPS's [7].

The method described in this paper, known as BURST PROCESSING (BP)[3] is the result of attempting to extend averaging techniques to a deterministic unary number representation, making sure that the complexity of the circuitry would be quite a bit lower than in WB representation, yet

perhaps not as low as in stochastic methods.   Two versions are discussed.
In one use is made of "quantized analog" circuits, better known as "multistate
logic" [2][23].   Perhaps the time has come to take such implementations more
seriously: The recent success of linear integrated circuits lets one hope
that 8- or 10-state devices will become common.   But burst processing is by
no means predicated on multistate devices; one can very successfully use
binary logic (in NWB form!)[9][10][15] for all computational cirucits--
this second approach is also treated in detail.

Before going over to a description of the fundamental principles
of burst processing, it should be clearly stated that this method is not
a panacea.   As a matter of fact it is somewhat wasteful of bandwidth: In
the 10-slot version we could represent the integers 0 though 10 by 4 WB
digits!   But the advantages of BP may well make this sacrifice acceptable.
Among the advantages are:

1.   Precision increases linearly with the number of time-slots.
     No correlation difficulties.

2.   Simple computational circuitry (typically less than 10% of
     WB systems).

3.   Possibility of on-line processing without staticizing the
     information: No synchronization is necessary.

4.   Great error tolerance because of averaging.

5.   Availability of a first appoximation at all times.

6.   Novel techniques for comparing, sorting, maximum-operations
     etc., leading to low cost equipment.

7.   Novel techniques for digital filters.

8.   RC-element emulation without capacitors, an important
     point for integrated versions.

It should be said that BP is only efficient if we can use crude approximations for our averaging process. Happily enough (see Section 4) such crude approximations are perfectly acceptable in the transmission of audio and video signals, in control-system computers (in which the output is averaged), in ranging and windowing equipment (sonar, radar) and, most importantly of all, in sampling devices for purely digital radios. As shown below, very encouraging results have been obtained in hardware realizations in all of these areas.

2. THE FUNDAMENTAL PRINCIPLES OF BURST PROCESSING AND ENCODING

The idea of burst processing (see Figure 2) is to perform very low precision arithmetic (typically on single decimal digits) and to use appropriate averaging procedures to obtain higher accuracy [2][3]. Figure 2 shows for instance how one can add 3.4 and 4.2 by decomposing 3.4 into a sequence of four 4's and six 3's, while 4.2 is decomposed into a sequence of two 5's and eight 4's. A one (decimal-) digit adder then gives--as successive sums--two 9's, two 8's and six 7's. The average of the latter is clearly 7.6, i.e. the sum of 3.4 and 4.2! The fundamental problem is obviously to produce automatically, in some circuit, the required integer sequences; we shall show below how this can be done.

THE AVERAGES OF LOW PRECISION ARITHMETIC
OPERATIONS CAN BE MADE EXTREMELY PRECISE.

EXAMPLE: 3.4 IS THE AVERAGE OF   4 4 4 4 3 3 3 3 3 3
          4.2 IS THE AVERAGE OF   5 5 4 4 4 4 4 4 4 4

| 4 | 4 | 4 | 4 | 3 | 3 | 3 | 3 | 3 | 3 | → | 1 - DIGIT ADDER | → | 9 9 8 8 7 7 7 7 7 7 |
| 5 | 5 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | | | | AVERAGE 7.6 |

THEREFORE   3.4 + 4.2 = 7.6

Figure 2

Fundamental Idea of Burst Processing

A possible format for representing the integers from 0 to 10 is a 10-slot frame (called a "block") with the integer n corresponding to n adjacent pulses at the beginning of the frame: This will be called a "compacted burst". Instead of using 10 slots one can, of course, also use m-slots per block; systems have been built with $4 \leq m \leq 16$. If we do not mention the value of m explicitly, it will be assumed that m=10. One of the interesting properties of this representation is that a "window" of length m always contains the same number of pulses, (namely n) (3) as long as we continue to represent n--quite independently of whether the beginning of the window coincides with the beginning of a block or not!

The so called Block Sum Register (BSR) shown in Figure 3a exploits the above "windowing property" in that the (quantized analog or m-state, here 10-state) output is proportional to the number of
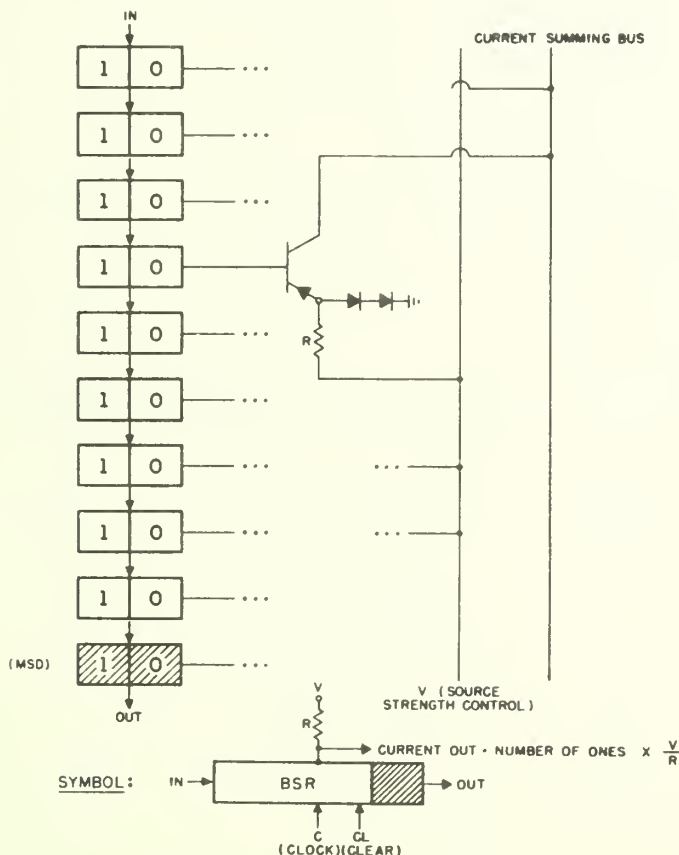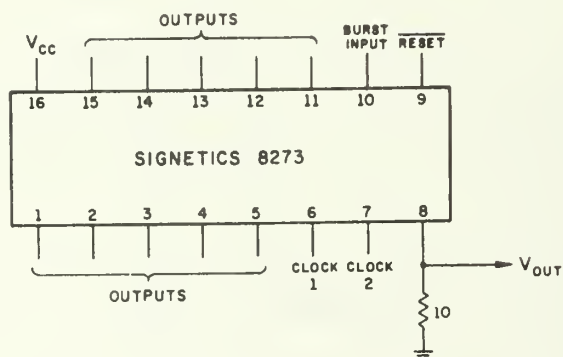

Figure 3a

Block Sum Register

"ones" in the shift register. Note that by adjusting V we can actually
multiply this number of "ones" by a predetermined coefficient; this
possibility is exploited in building digital filters (see below) using
BSR's.

If burst processing were to be adopted on a large scale, it
would be trivial to implement a BSR according to Fig. 3a through a
semiconductor house, instead of building it from a shift register and
current sources. If an accuracy of 2% per step is sufficient, Ma has
shown that we can use a sensing resistor (e.g. 10Ω) in the ground return
of certain shift registers [23]. The best performance was obtained from
a Signetics 8273 as shown in Fig. 3b: Although the variation from chip
to chip was from .0085V to .010V per step, for a given chip the linearity
was astonishingly good, namely less than 2% variation from step to step!

OUTPUTS

BURST
INPUT   RESET

V_{CC}

| 16 | 15 | 14 | 13 | 12 | 11 | 10 | 9 |

SIGNETICS 8273

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |

OUTPUTS

CLOCK CLOCK
1   2

V_{OUT}

10

SIGNETICS 8273 — 10 BIT SERIAL IN PARALLEL OUT SHIFT REGISTER
MINIMUM FREQUENCY - 25 MHz

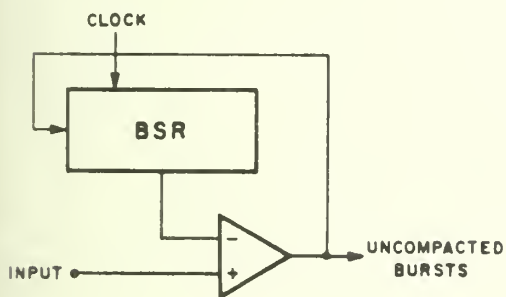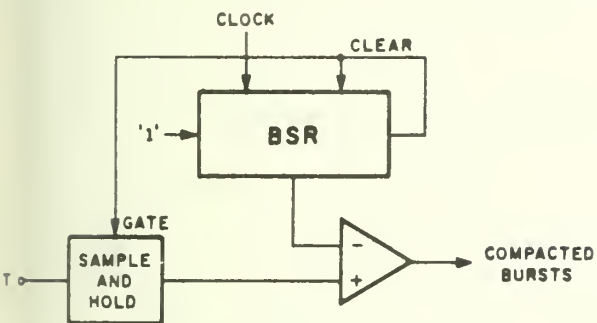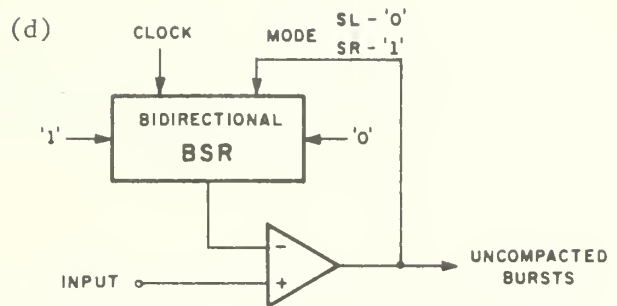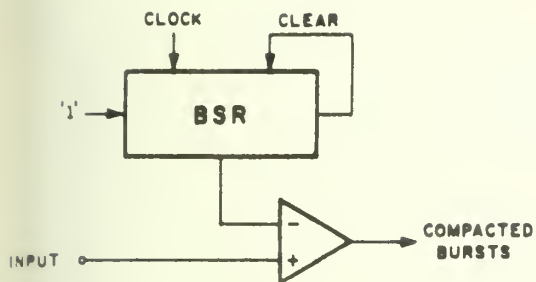| NUMBER OF ONES	SAMPLE OUTPUT VOLTAGES (±.0002 VOLTS)	
10	.144	.150
9	.153	.159
8	.162	.168
7	.171	.177
6	.180	.186
5	.189	.195
4	.198	.204
3	.207	.213
2	.216	.222
1	.225	.231
0	.234	.240

Figure 3b

Signetics 8273 used as BSR
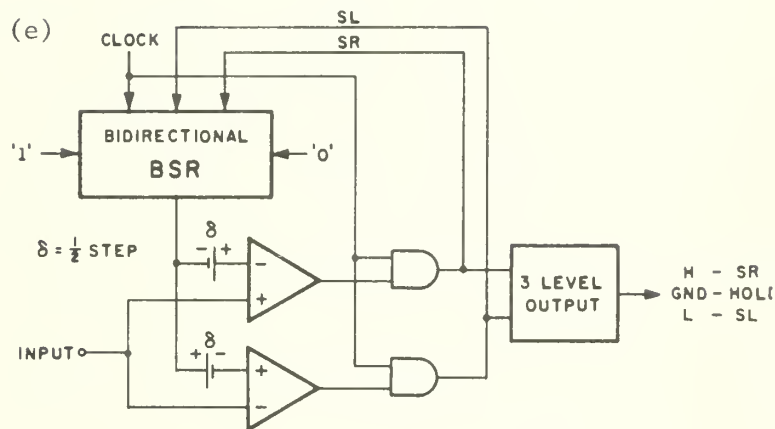
Figure 4

Burst Encoders

It must be mentioned that the compacted burst format, although usually easier to handle, is by no means a necessity. Figure 4 shows a variety of encoders studied by Wolff [15][16]. The first one (Fig. 4a) is the original ramp encoder which consists of a BSR connected as a stair-step generator and a comparator. It does actually furnish compacted bursts. Because the stairstep generated by the BSR samples the input at a time dependent on the input voltage, the input must change by less than one level of quantization during one stairstep. This obviously limits the maximum input frequency. With the addition of a sample-and-hold circuit (Fig. 4b) the bandwidth can be increased to the Nyquist limit.

A different encoder using essentially the same components is the delta block encoder (Figure 4c). Here the BSR tracks the input signal by clocking in "ones" or "zeros" depending on whether it is below or above the input. Unfortunately the BSR only changes its output if the input bit is the opposite of the final bit: The tracking depends on the history of the input signal! Figure 4d shows a way out: We use a bidirectional BSR with a "one"-feed on the left and a "zero"-feed on the right. Fig. 2e shows a not uncommon 3-level version called "bibursts" [15] which has synchronization and bandwidth advantages. Here we transmit a positive or negative pulse when the input differs from the BSR value by more than half a step. The receiver therefore does not need a clock: It derives it's clock from the edge of the input pulses and simply freezes its value if none are coming in!
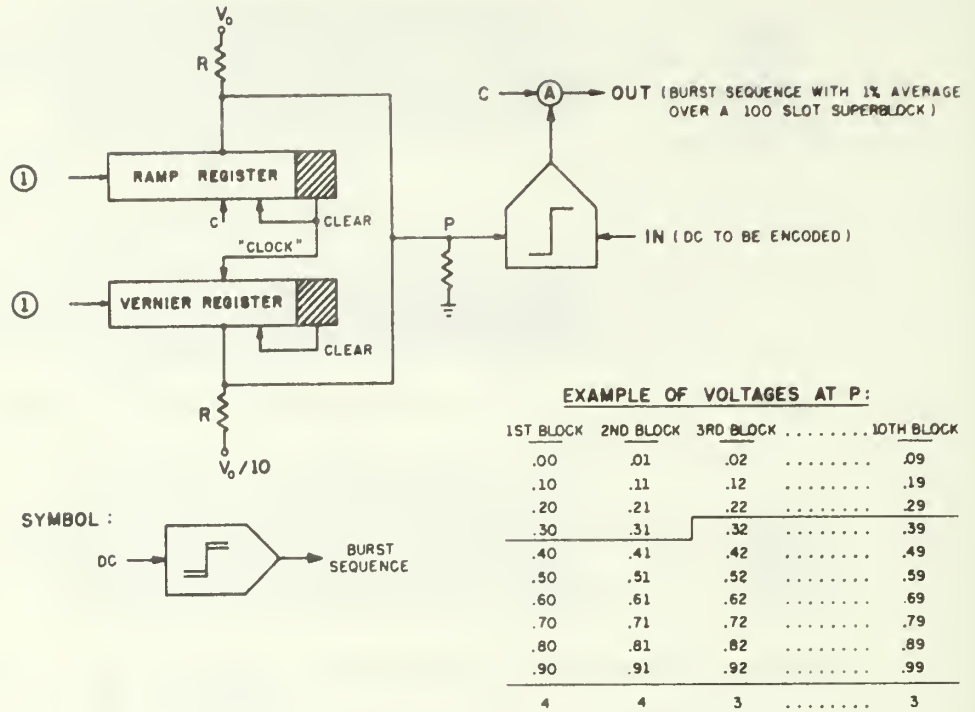
Figure 5

Burst Encoding and Decoding

In Figure 5 we show the action of a ramp-encoder when the input
varies and the reconstituted signal is taken from a BSR.   It should
be noted that a window of length 10, sliding along the transmitted sequences
gives, at any moment, the most recent approximation and that it interpolates
in so doing.   Voice transmission has been shown to be feasible with only 3
slots and a clock-rate of 10KHz.

Figure 6

· Vernier Encoder

As mentioned before, it is of paramount importance to produce
the sequence of bursts which represents a number of higher precision than
.1 (i.e. 10 slot system) by an automatic device. A simple circuit is a
combination of two BSR's successively filled with "ones", in which one
BSR--the "vernier register"--runs at 1/10 the speed of the main BSR, i.e.
the "ramp register":   Each time the ramp register is cleared (when the
"ones" attain the most significant digit), the vernier register adds to
the output current of the ramp register one tenth of one step of the former.
Normalizing the combined output current (or the voltage at P!) to 1, the
table in Figure 6 shows how the slow shift upwards of the stairsteps
produces first the longer bursts, then the shorter ones and precisely the
requisite number! All that is necessary is to compare the voltage in P
with the voltage to be encoded--also normalized to 1--and to switch on the
clock pulses by an AND-gate as long as the voltage to be encoded (.32 in

the Figure) is higher than the comparison voltage. This device is called a <u>vernier Encoder</u> [2] [3].

One of the advantages of burst processing is that error-pulses can be reasonably well absorbed because the BSR's show averages. In case we use compacted bursts, one can improve the situation by taking a <u>majority vote for every 3 adjacent slots</u>: This fills in 1-slot gaps and suppresses single pulses. It has been shown that under some noise conditions (10% error rate and above) this system gives results superior to Read-Muller codes.[11]

It should also be noted that in case of compacted bursts we can transmit pulses of varying width constituting <u>the envelope of the bursts</u>: burst processing is quantized pulse-width modulation. On the receiving end we then simply AND the envelope with the sytems clock.

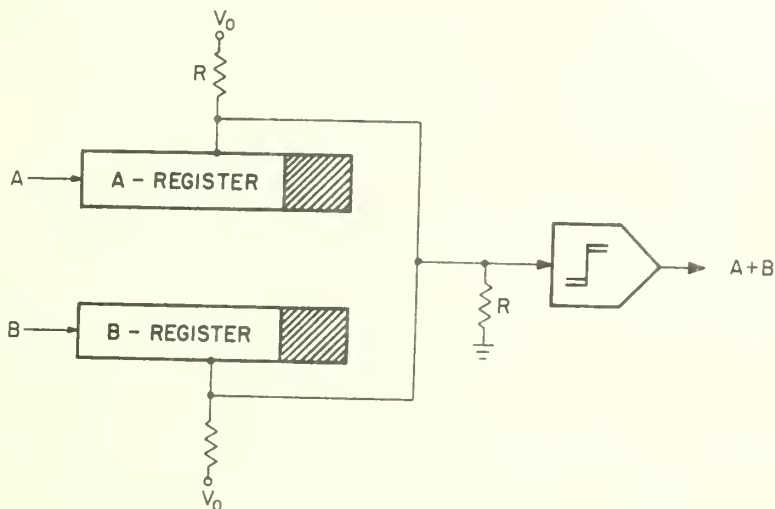3. <u>ARITHMETIC UNITS FOR BURST PROCESSING</u>

Figure 7

Quasi Analog Burst Adder

Figure 7 shows the most direct way of performing addition

(and subtraction when we take the difference of the output of the

BSR's) [2][3]: We simply use analog addition of the quantized analog

output of BSR's, the result being re-encoded by a ramp encoder or a

vernier encoder. Scaling in the quasi analog adder can be obtained by

modifying R. The semiconductor houses are perfectly capable of making

8-, 10- or even 16-state elements, but strangely enough most engineers

are reticent to use these multistate designs: It is therefore appropriate

to consider purely logical implementation using standard binary techniques.

Figure 8 shows a so-called selector adder [9] for compacted bursts: Note
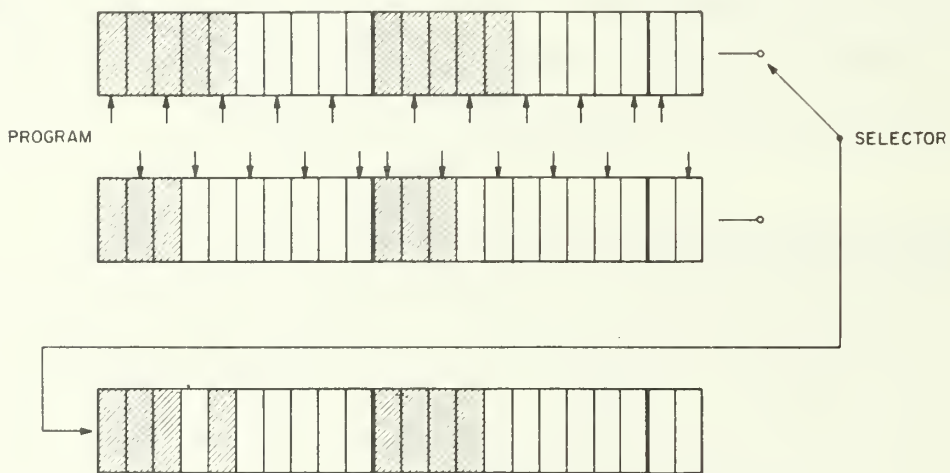
NOTE 1: THE SELECTOR IS PROGRAMMED TO SWITCH PHASE AT THE END OF EACH BLOCK.
NOTE 2: THE OUTPUT IS UNCOMPACTED AND MUST BE USED TO SHIFT ONES INTO
        AN ASSEMBLY REGISTER.

Figure 8

Selector Adder

the analogy with the stochastic adder of Fig. 1b. In order to eliminate any

bias for odd numbers of pulses, the selector switches phase at the end of

each block. The output is uncompacted--in order to obtain a compact output

we shift "ones" into an assembly register whenever a "one" occurs in the

bottom sequence.

Logical arithmetic units of many different designs have been built. One of the more sophisticated ones uses the so-called carousel multiplier/divider (CMD) [9][24] shown in Fig. 9. The fundamental idea of
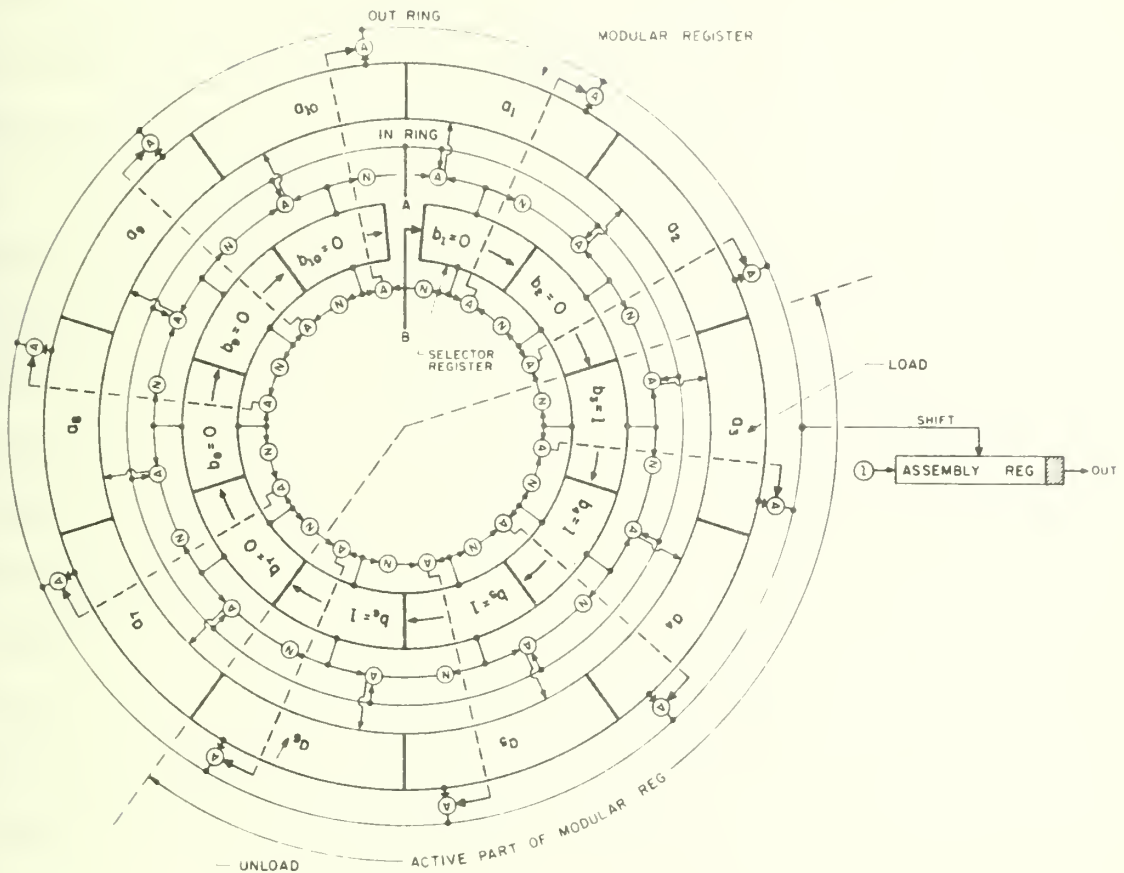

Figure 9

Carousel Multiplier/Divider

the CMD is that both multiplication and division of burst sequences can be thought of as the "filling up" of a register (called MODULAR REGISTER in Figure 9) by a stream of pulses, being careful to note the occurence of overflow. In case of the multiplication of A by B, we make the modular register of length 10 and shift into it as many blocks of B as indicated by A: counting the number of overflows, we then obtain AB/10. Note that if we leave the modular register uncleared at the end, we shall obtain an exact value when we average!

For division A/B we simply make the modular register of length B and note its overflow as we shift in a fixed number (e.g. ten) blocks of A: Of course, only the "ones" in A produce the filling of the modular register. The slightly exotic design of Figure 9 actually adjusts the length of the modular register dynamically by walking the "ones" in B through a SELECTOR REGISTER: That portion of the modular register opposite the ones in the selector register is the active part of the modular register. By rotating "load" and "unload" gates (determined by detecting the 01 and 10 edges of the rotating active part!) we transfer the "ones" of A onto the rotating active part of the modular register and also detect the overflow. The situation can be visualized by thinking of the flipflops in the active part as freightcars on a circular track, the train being filled up - while it moves - from the last car forward and emptied, as a block, whenever the car next to the locomotive is filled. The reason that the dynamic adjustment of the modular register is desirable is that we then actually form $(\overline{A}/\overline{B})$. Note that often we require $(\overline{A/B})$: If we impose the condition $A/B \geq .5$, it can be proved that the two averages differ by less than 5 percent in the 10-slot system.
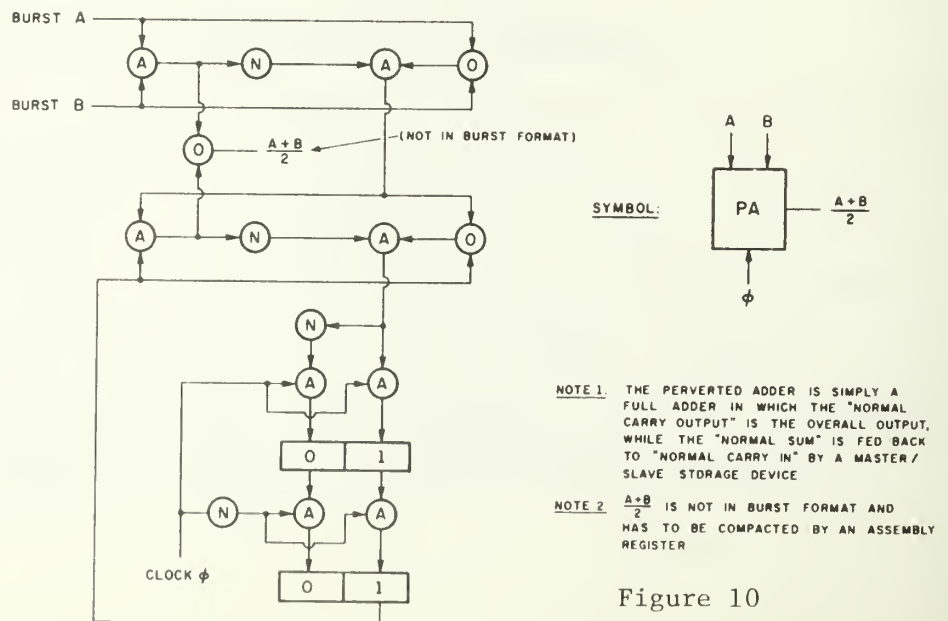

SYMBOL:

NOTE 1. THE PERVERTED ADDER IS SIMPLY A FULL ADDER IN WHICH THE "NORMAL CARRY OUTPUT" IS THE OVERALL OUTPUT, WHILE THE "NORMAL SUM" IS FED BACK TO "NORMAL CARRY IN" BY A MASTER/SLAVE STORAGE DEVICE

NOTE 2 $\frac{A+B}{2}$ IS NOT IN BURST FORMAT AND HAS TO BE COMPACTED BY AN ASSEMBLY REGISTER

Figure 10

Perverted Adder

It was noted by Taylor and Tietz [11][24] that it is possible to modify a serial full-adder in such a fashion that it furnishes an uncompacted sum of two (uncompacted) bursts with a normalizing factor of 1/2. Figure 10 shows why we call the arrangement a perverted adder (PA): What is normally the carry output of a serial adder gives the (normalized) sum while the sum output in normal operation becomes the input to the carry-delay circuit. The carry delay is in effect a master/slave D-flipflop pair (symbolized by two RS flipflops and appropriate gates), which delays the carry by one clock cycle and then re-inserts it in the next cycle of the adder. Note that contrary to the selector adder, we have several collector delays and that the carry feedback limits the speed. But there are also very attractive features, in particular the fact that we can cascade many PA's if necessary!
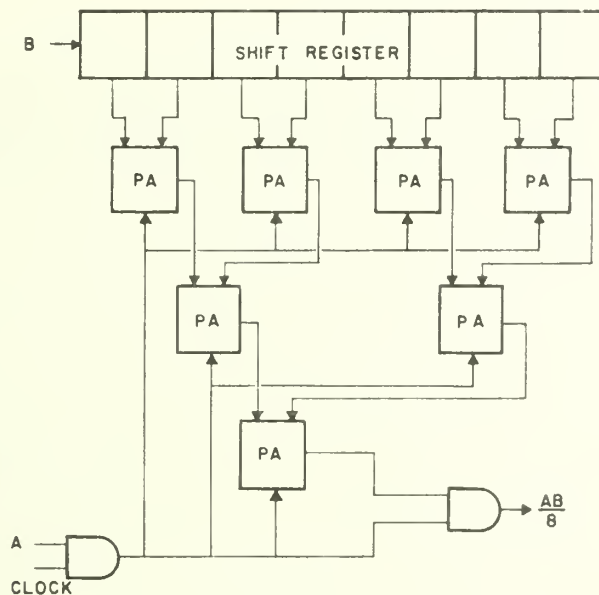

Figure 11

PA Multiplier

The ease with which PA's can be cascaded is used in the <u>PA-Multiplier</u> of Figure 11. Here we use a tree of PA's to (dynamically) add all digits in A whenever B has a "one". It is not hard to see that when we use all "ones" in B, we obtain AB/8 at the output. The figure shows the arrangements for an 8-slot burst format, because this is more efficient than the standard 10-slot format for a tree-structure, but it is, of course, possible to design a 10-slot version!

We have not commented on the complexity of AU's for burst processing: By optimizing the design (LOCOBURST Project) [15][24] we have been able to imitate an 8-bit microprocessor (10MHz clock) with about 10% of the gate count. In these times of ultra-cheap hardware this may not be so impressive, but the critics often forget that a simplification by a factor 10 means also 10 times less power consumption, 10 times less space, and 10 times more reliability!

4. <u>BURST DIGITAL FILTERS, CONVOLUTION, PREDICTOR THEORY and RADIOS.</u>

Like stochastics, burst processing was initially a method in search of an application. For stochastics the solution of systems of differential equations (and therefore modelling of large systems) seems to be most attractive. For burst processing one of the more promising fields is that of digital filtering. Fig. 12 shows--somewhat whimsically-- why such an application is desirable: When averages of many (more or less random) numbers are calculated, each number can be a crude approximation, in particular a 8- or 10- slot burst approximation!

FOR RANDOMLY DISTRIBUTED NUMBERS THE AVERAGE CAN BE
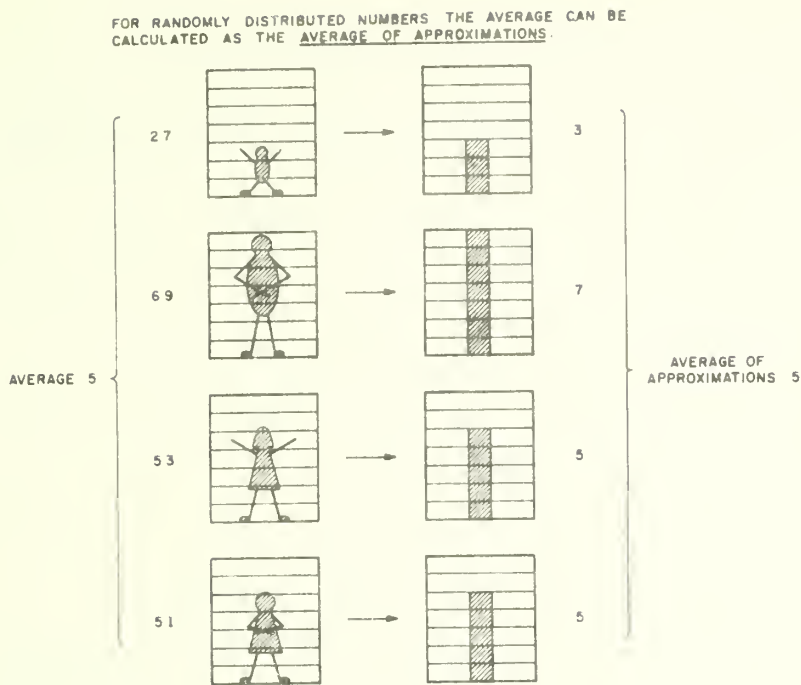CALCULATED AS THE AVERAGE OF APPROXIMATIONS.

Figure 12

Why Burst Processing Works

We have concentrated mostly on realizing FIR (Finite Impulse

Response) filters, i.e. filters in which delayed versions of the signal are

multiplied by certain constants and then added [11]: No feedback from output

to input is allowed as in IIR (Infinite Impulse Response) filters. The

reason for this limitation is that the noise problems in IIR filters are much

more severe and the (crude) burst approximations are therefore less

attractive. Nonetheless IIR filters have been shown to be viable, for instance

in Pitt's PREDICTORBURST project discussed below. The theory of designing

FIR digital filters from an analog version is well known and leads to a

layout as shown in Fig. 13a. To implement such a filter, we simply replace

the circuit delays z^{-1} by n-bit shift registers (typically n=8, 10 or 16)

and multiply their burst contents (i.e. the number of "ones") by appropriate

constants c_1, c_2, etc. as shown in Fig. 13b.
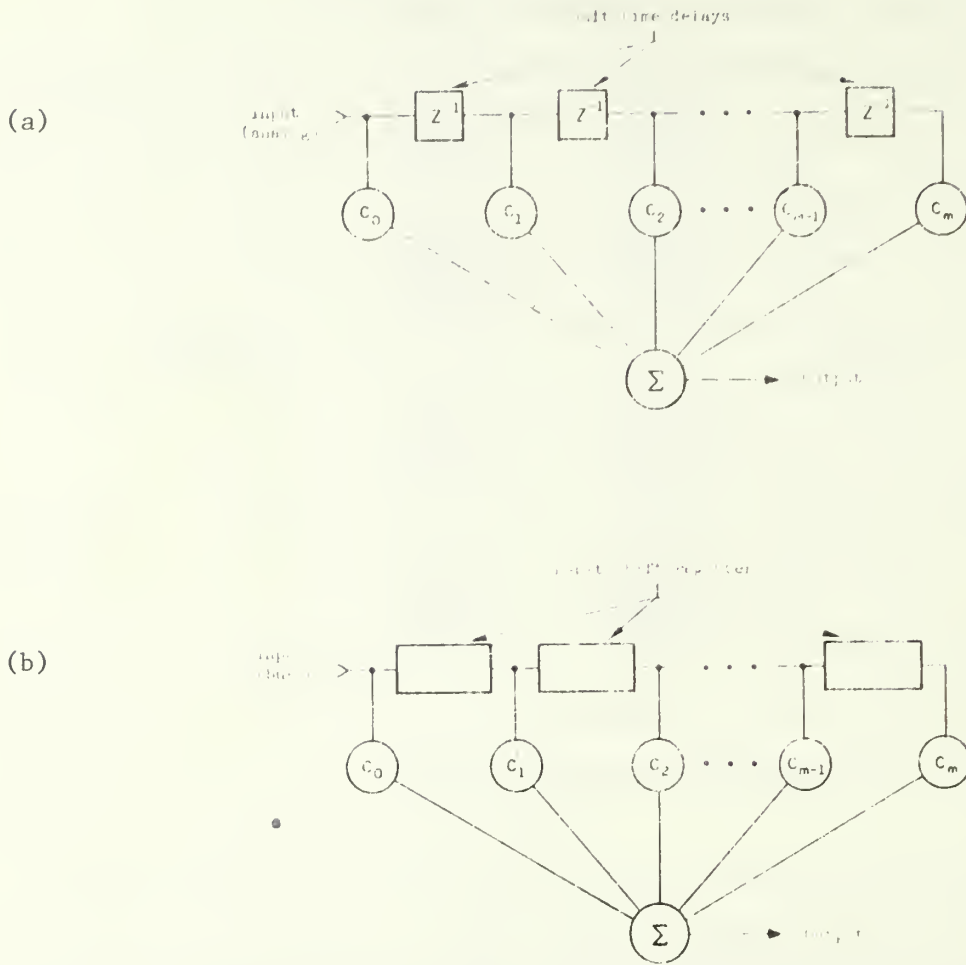
(a)

(b)

Figure 13

General FIR Filter (a) and Burst Version (b)

As in our arithmetic units there is again a quasi-analog and a purely digital way of realizing Fig. 13b. In the former case c_1, c_2 etc. are simply the return voltages on BSR's and we use analog summation. Fig. 14 shows such an application (developed by Xydes) for an on-line Fourier Transform Unit used in a rather sophisticated frequency analyzer for speech (BURFT) [15] [17]. Fig. 15 shows an adaptive system (PREDICTORBURST) to calculate the predictor coefficients a_i (only stage i=2 is shown explicitly) in view of bandwidth compression of human speech--as is well-known the a_i's vary quite slowly. MDAC is a multiplying digital-to-analog converter

which sends $a_2 \cdot s_{n-2} \; [+ \, a_1 s_{n-1} + a_3 s_{n-3} + \ldots]$ to a summing amplifier. The latter forms the error signal. Note the feedback from the error-output to the counters storing the a_i's.
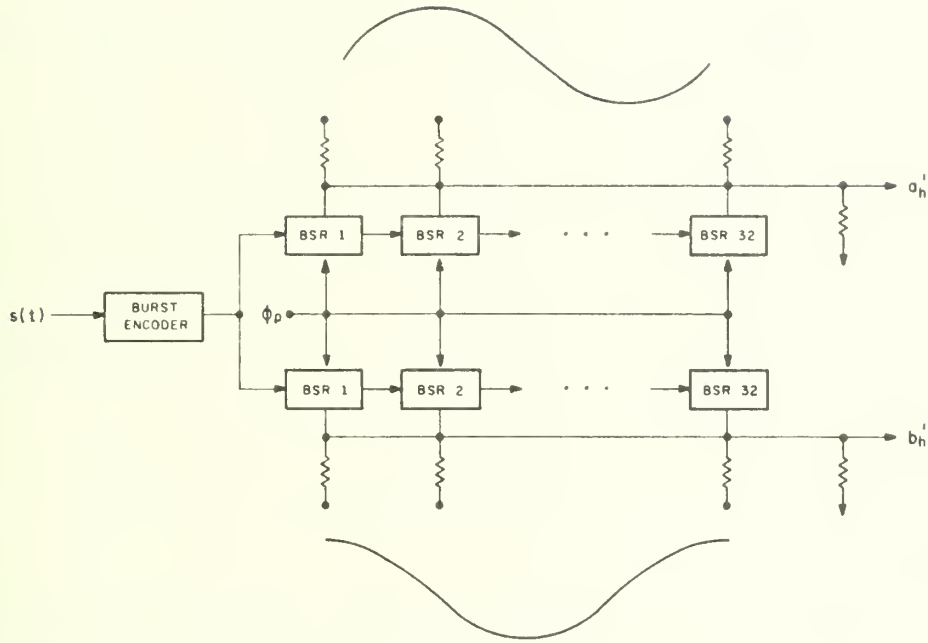

Figure 14

BURFT Fourier Transform Unit

$$u = v_0 - \sum_{i=1}^{p} v_i = s_n - \sum_{i=1}^{p} a_i s_{n-i} \triangleq e_n$$
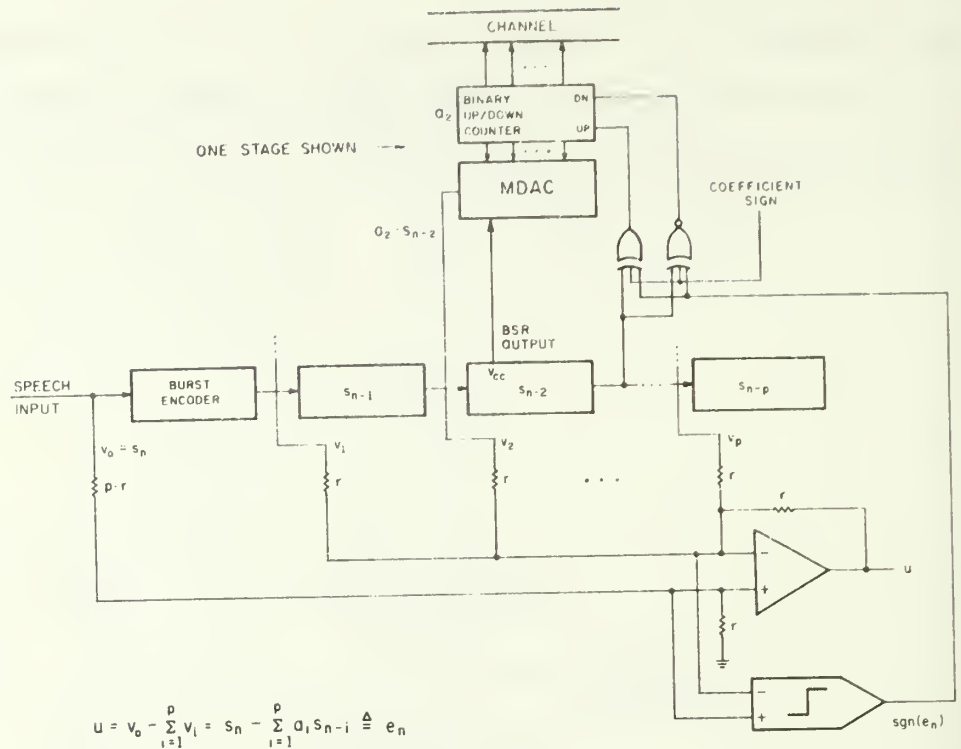
Figure 15

PREDICTORBURST Unit

In order to obtain a purely digital version of a FIR burst
filter, we can again revert to a perverted adder (PA) design: Here the
coefficients c_1, c_2... etc. are supposed to be small integers and their
influence is realized by appropriate fan-outs inside the PA tree [18].
Fig. 16 shows the practical layout of a Hamming Weighted Filter studied
by Wells. Two clock lines (CKS and CKF) are used because the filter is
actually multiplexed! In conjunction with some additional burst filters
to suppress the periodic peaks due to sampling at 125 KHz, the response
is down 39 db at 8 KHz from the center (null-) frequency, and down by
better than 70db at 125 KHz. This is comparable to what one obtains
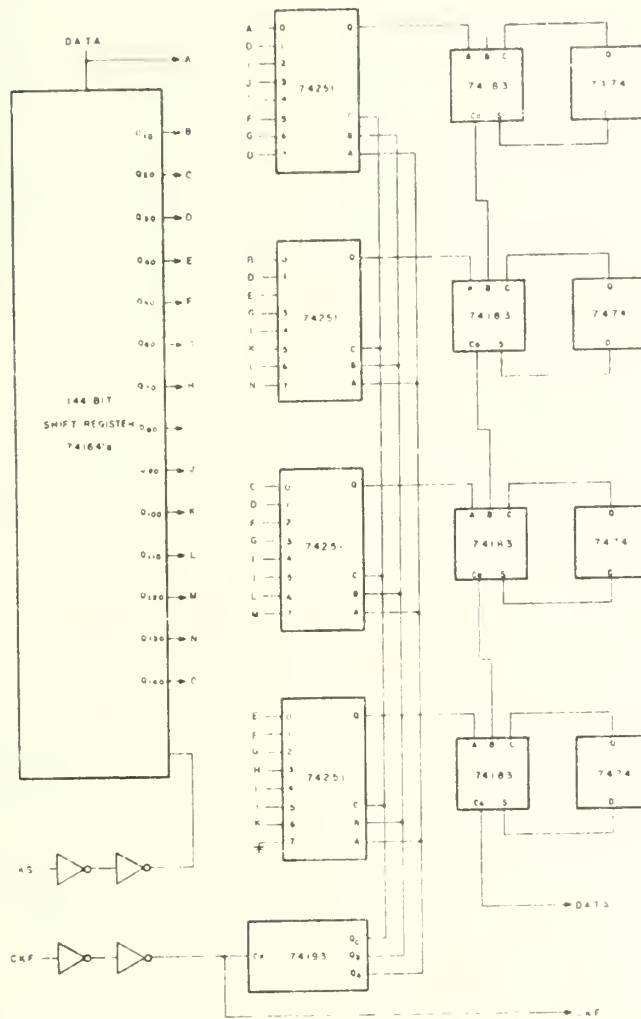in good communication equipment.

Figure 16

Hamming Weighted Burst Filter

From the outset we became very interested in digital radios and used comb-filters for tuning [5] [9]. The principle is shown (for AM) in Fig. 17. The idea is that if we sample at the frequency of the desired station, we shall obtain constructive interference of the samples for that station, while other stations will be subject to destructive interference. Here it must, of course, be assumed that during the integration over about

100 cycles the amplitude remains essentially constant: This is the case

for speech and a carrier above 1 MHz, a condition always met in real life.
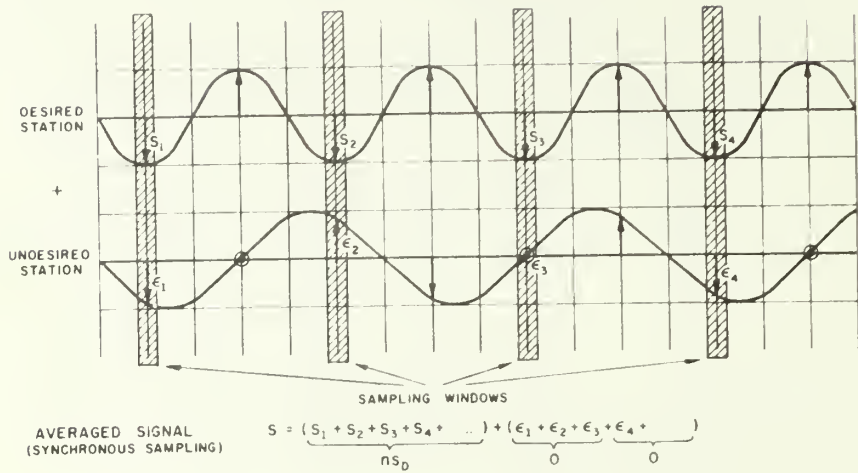
Figure 17

Principle of Interference Tuner

In practice it is awkward to operate with variable frequency clock in order

to obtain tuning. Fig. 18 shows how this can be avoided by using (delaying)

shift registers of variable length: Tuning then corresponds to adjusting the

delays so that from BSR to BSR we have exactly one period of the desired

station! To extract the AM modulation, Noble simply averaged the tuned

signal, for instance by running it into a counter and watching the overflow.
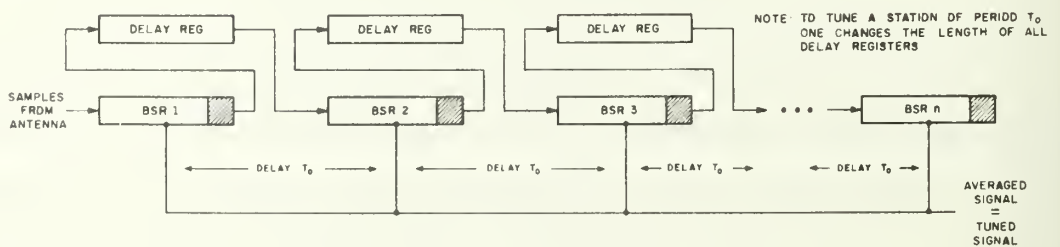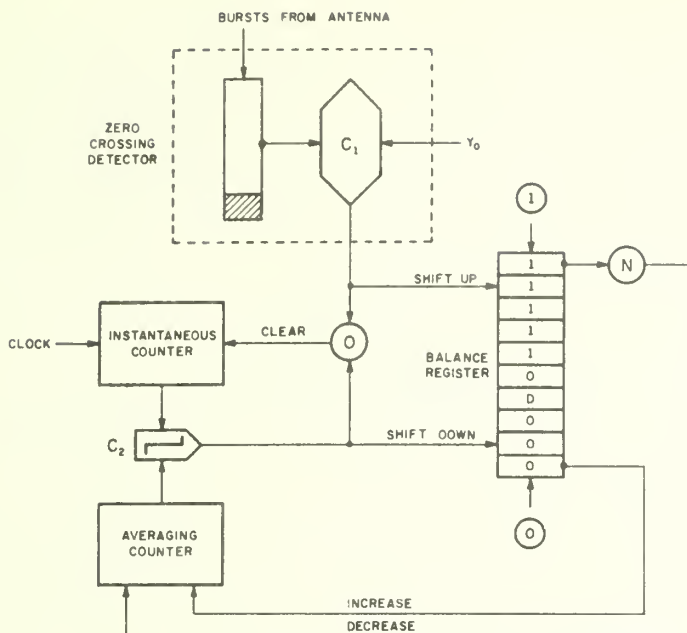

Figure 18

Delay Register Tuner

BURSTS FROM ANTENNA

ZERO CROSSING DETECTOR

C_1 — Y_0

SHIFT UP

CLOCK — INSTANTANEOUS COUNTER

CLEAR — O

BALANCE REGISTER

SHIFT DOWN

C_2

AVERAGING COUNTER

INCREASE

DECREASE

1

N

1
1
1
1
1
0
D
0
0
0

O

NOTE 1 IN ESSENCE THE CIRCUIT SIMPLY DETECTS WHETHER THE NEXT ZERO CROSSING OCCURS (OR NOT) BEFORE THE INSTANTANEOUS COUNTER REACHES THE PREVIOUS AVERAGE BETWEEN ZERO CROSSINGS. THE BALANCE REGISTER MODIFIES THE AVERAGE

NOTE 2 THE WIDTH OF THE WINDOW OF COMPARATOR C_1 CORRESPONDS TO ONE PULSE OF A BURST

NOTE 3 COMPARATOR C_1 AND (SIMPLIFIED) COMPARATOR C_2 CAN BE REPLACED BY DIGITAL DESIGNS

Figure 19

PLL for FM Demodulation

To demodulate FM we must determine the average frequency of

the (tuned) antenna signal. This can be done by building a burst-implemented

phase-locked-loop (PLL) and watching the average time between zero crossings

of its output [9][18][20].

The PLL-design in Figure 19 studied by Robinson and Mohan starts,

on top, with a zero-crossing detector. Although we indicate a BSR and a

comparator in this position, it is clear that we can use a purely digital

design. The game is now to count clock-cyles between zero-crossings in an

"instantaneous counter". If the count is high, we increase the averaging

counter; if it is low, we decrease it. Of course, such a feedback system

must have some inertia built into it. This is done by delaying the increase/

decrease decision in the "balance register", which has its 1/0 boundary

hop up and down, but only large and repeated hops lead to "1" slipping
out on top, or "0" on the bottom. It is the "slipping out" which modifies
the averaging register in the appropriate direction. Clearly the contents
of the averaging counter can be used to retrieve the FM.

5. PICTURE, INDICATOR-AND SEQUENCY-PROCESSING

This paper cannot cover the many designs in the burst area
which have been examined at IEL during the past 3 years: The bibliography
gives a complete list. But 3 projects stand out because of the insight
they afforded us into the pros and cons of burst processing and also into
future generalizations.

In Bracha's WALSHSTORE [21] project we examined the feasibility
of storing the "electronic hologram" of a binary input picture in such a
way that the destruction of a large percentage of the memory would simply
correspond to a lack of definitions of the reconstituted input. This
objective was attained by using a two-dimensional Walsh-Transform. Burst
processing was used (in conjunction with weighted binary techniques)
because the input came from a CCD-type camera which essentially shifted
out bursts. But the storage of the transform, (obtained by burst processing)
was done in binary: The storage of a number in non-weighted unary fashion
would be prohibitively expensive.

In Gostin's INDIRAD [15][25] project we used a spatial version
of bursts: In a set of 7 wires we energize just one to indicate the numerical
value of waveform-samples taken at times in quadrature, i.e. for sin t = $\pm$ 1
and cos t = $\pm$ 1. The advantage of such an Indicator Representation is that
very fast arithmetic becomes trivial: All we have to do is to realize a
table-look-up scheme (for sum, product etc.) in hardware. The averaging at
the end then smoothes the results. Fig. 20 shows the block-diagram of INDIRAD.
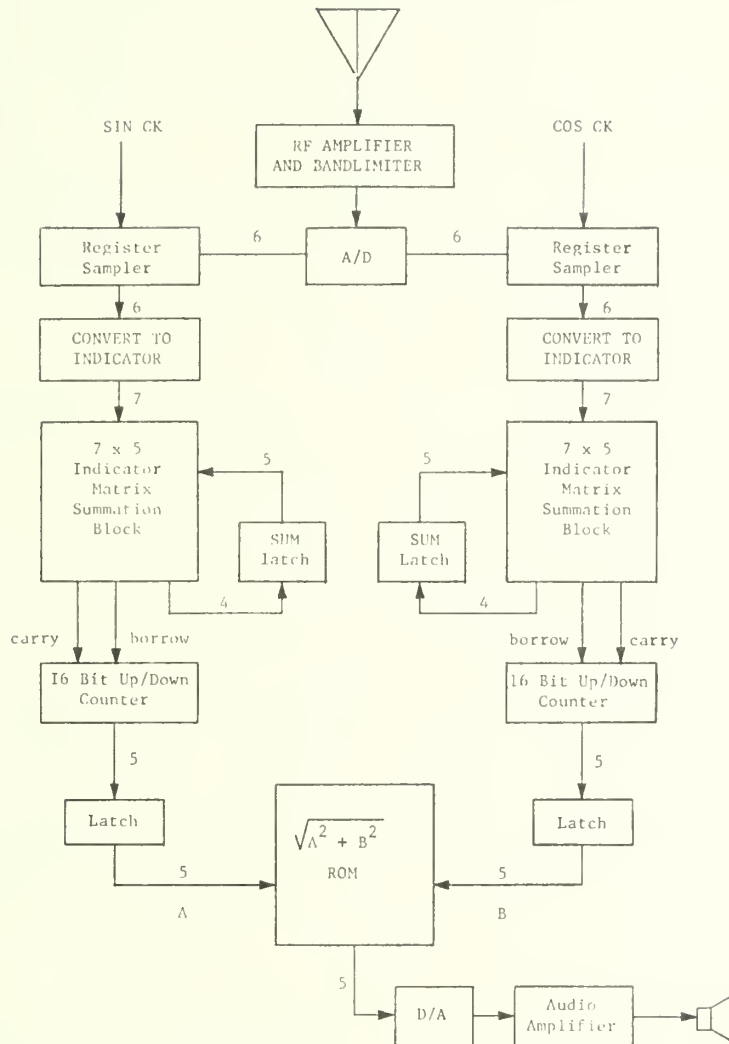
Figure 20

Block Diagram of INDIRAD

We have already mentioned that if a 10-slot burst system is replaced by weighted binary, we gain a factor of 2 1/2 in bandwidth. Sequency Processing [19] tries to gain bandwidth for the average case ($\rightarrow$ 5 pulses in 10 slots) by abandoning the fixed frame format--this gives a factor 2 on the average, making it nearly the equivalent in bandwidth of weighted binary. The actual format is shown in Fig. 21 . Again we have a quantized
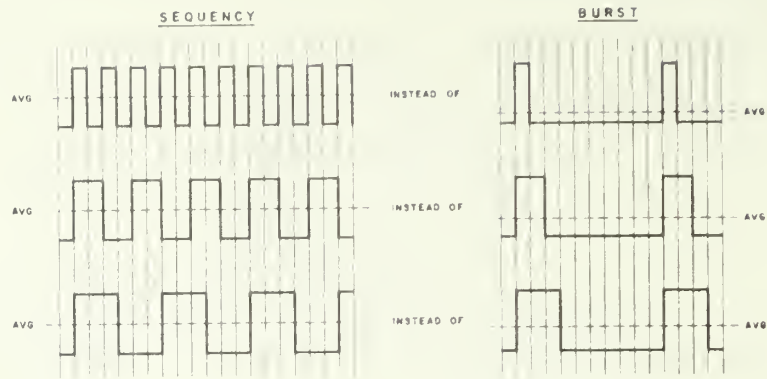
Figure 21

Comparison of Burst and Sequence Representation

pulse-width modulation, but here we use a variable frame reference (namely
the last 0→1 or 1→0 transition). Successive frames are inverted with respect
to each other: The average is always one-half of the full swing--this has
advantages in CW applications. Although the system updates more frequently
than burst processing (as a matter of fact: It has a binary version which
updates faster than any other sytem...), we must realize that arithmetic
units are more complex, mostly because we have no exact equivalent of the
"windowing property".

Finally we should note that burst processing uses only a small
number of standard elements (BSR's, comparators, counters, ANDs, ORs, and
NOTs) and that designing with it is rather easy. In case relatively
untrained personnel has to be used for design and maintenance, this "modular
kit" feature could be very attractive!

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Additional information may be obtained from the Quarterly Progress
Report of the IEL and the Annual Reports of the Department of Computer Science
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15. Supplementary Notes

16. Abstracts

   To multiply two numbers with 7 bit (i.e. 1%) accuracy a 2000 transistor microprocessor needs about 10 clock-periods. A stochastic computer gives the same accuracy (within one standard deviation) in 10^4 clock periods--but it only uses a 2 transistor AND for the operation. For the last 4 years the Information Engineering Laboratory in the Department of Computer Science at the University of Illinois has examined a "compromise" called BURST PROCESSING, which uses deterministic methods (like a microprocessor), but averages (like a stochastic machine). The fundamental idea is to perform 1-decimal digit arithmetic and to obtain accuracy by averaging over various inputs. For example 3.4 would be treated as 4444333333 and 6.2 as 7766666666. Using the insight that the average of a sum is the sum of the averages, we can use a simple adder which forms (4 + 7), etc., the average being 9.6 = 3.4 + 6.2!

17. Key Words and Document Analysis. 17a. Descriptors

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17c. COSATI Field/Group

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